

SIEMENS DIGITAL INDUSTRIES SOFTWARE

Understanding formal methods for use in DO-254 programs

Executive summary

This paper seeks to take the mystery out of the use of formal methods for hardware verification. In this discussion, we will first explain formal methods as clearly and concisely as possible. We will then look at the state of the industry and the changes over the last decade or so that have enabled the widespread use of formal methods for hardware verification. With this knowledge in-hand, we will examine and explain the contents of DO-254 Appendix B 3.3.3 "Formal Methods." Finally, we will bring this information together and provide recommendations for using formal methods on a DO-254 project.

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I Introduction

Formal Verification is one of the most misunderstood areas of DO-254. It is one of the few actual design or verification methods named in the RTCA/DO-254 document (Appendix B) and is in fact listed as an appropriate method for the “Advanced Verification” requirements for Level A/B designs. The problem is that the content of Appendix B is extremely difficult to understand. The text in this section was largely taken from texts or papers on formal methods intended more for the academic rather than today’s typical user. In addition, it is also too oriented towards formal verification for software. Add to this, the information is over 20 years old. This has resulted in fear (in the minds of the project team who wants to use it on their DO-254 programs but don’t want to increase their project’s scrutiny) and unease (for the certification authority who sees its use called out on a DO-254 program but does not really understand this use or its purpose).

This paper seeks to take the mystery out of the use of formal methods for hardware verification. In this discussion, we will first explain formal methods as clearly and concisely as possible. We will then look at the state of the industry and the changes over the last decade or so that have enabled the widespread use of formal methods for hardware verification. With this knowledge in-hand, we will examine and explain the contents of DO-254 Appendix B 3.3.3 “Formal Methods.” Finally, we will bring this information together and provide recommendations for using formal methods on a DO-254 project.

I Formal methods overview

Even though the practical application of formal methods was in its infancy during the original writing of DO-254, the authors of DO-254 certainly understood the potential of formal methods in terms of enhancing design assurance. This section provides some foundational information that can help you understand why the DO-254 authors felt formal methods were pertinent and useful in terms of aiding design assurance.

What are “Formal Methods”?

Formal methods make use of exhaustive mathematical algorithms to verify the functional correctness of a design against its requirements. Because the process is exhaustive, the verification answer to the question “does this design meet this requirement” is guaranteed to be complete. That is, if design can exhibit any undesirable behavior, formal methods will point them out. On the other hand, if formal can prove that no such undesirable behavior exists, then formal methods will say so.

Contrast this with commonly used simulation techniques, which is considered a “probabilistic” approach. This means the tool itself cannot guarantee that all undesirable behavior will be identified. It’s entirely up to the user to think of all possible undesirable behavior and test each one individually.

This is best explained with an analogy to doing a math problem. Consider solving the equation $2X^2 - 8X + 5 = 0$ for X. You can brute force and estimate an answer by trying various combinations of X and narrowing down the possibilities. This is similar to how you’d write tests using a directed test simulation approach. Your attempts might look something like this. (X is the input, Y is the output. According to the above equation, we want Y to equal zero, so our challenge is to find the correct value of X).

	X	Y
Test #1	0	5
Test #2	1	-1
Test #3	2	-3
Test #4	3	-1
Test #5	4	5
Test #6	5	15
...		

From your test results, you can see that Y is 0 when X is somewhere between 0 and 1, and again somewhere between 3 and 4. (Note if you stopped testing after X=1, you also may have thought there was only one answer!). If you’re happy with that estimation, that is fine. But if you want to find the exact answer, you’d simply plug the numbers into your calculator and use the quadric formula to solve exactly:

$$X = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

A high-end calculator would provide both a graph of the function and exact values for X (X = 0.775 and X = 3.225). When the calculator comes back with the solution, you know that it is accurate and complete.

This is how formal methods work. Formal methods use mathematical principles in this very same way to provide a complete and repeatable answer. The question formal methods answers is whether a design model implements its intended function.

Formal methods value for DO-254

Today, many companies are using formal methods as they understand how it uniquely offers value due to its ability to improve design quality. It is a technique unlike any other in that it can perform some very essential roles for safety-critical and mission-critical designs. For example, it is possible with formal methods to exhaustively verify safety-critical properties. Likewise, with formal methods you can explicitly check for situations that you want to ensure never happen. You can also easily find unintended and unanticipated design behaviors with formal methods. This can best be shown through an example.

Consider the design of an FPGA that controls the reverse thrusters of an aircraft. A safety- consideration of this design would be to ensure that the reverse thrusters NEVER fire when the aircraft is airborne. This would likely result in a catastrophic failure of the system.

To ensure this detrimental situation could never happen, you would want to exhaustively verify the design to prove that there are absolutely no scenarios where this could happen. With formal methods, you would check the design to ensure that

the property “the reverse thrusters can never fire while in mid-air” always held true. Formal methods would tell you all the scenarios that violate that property. This is the true power of formal methods.

With simulation you can verify expected behavior given defined circumstances, but you can never fully verify unexpected conditions. Yet simulation has been the perfectly acceptable approach to verification. By augmenting traditional simulation approaches with formal methods, confidence that the design performs its intended function (a.k.a., design assurance) improves.

Inputs to formal

Achieving design assurance as demonstrated above using formal methods is much easier than most people realize. All it takes is a formal engine (that runs mathematical analysis), the design model, and the requirement. The design model itself is just the standard RTL model (typically VHDL) that is developed during the “detailed design” phase, simulated, and then synthesized. This model requires no additional work to be used with formal methods.

The requirement would normally be stated in English (or the natural language used in the project) where it is captured and traced throughout the process. In order to use this requirement with formal methods, the requirement would need to be written in a formal property specification language. (You can think of a property as the same thing as a requirements).

Today there are several industry standard property languages, which are commonplace and well-understood. Once this formal property description is written, it should be reviewed against the original requirement for accuracy. (In fact, this provides another layer of design assurance in the flow, as translating a requirement to a formal language is a very good exercise in requirements validation, as the translated property must be unambiguous and verifiable. Going through this process is an excellent double-check on the validity of the requirement).

Once you have your RTL coded and your requirement written as a formal property, you can run formal. This is really all it takes to exhaustively verify a safety-critical property. Every violation of the property identifies unexpected behavior of the design that must be fixed.

Why the confusion and why don't more people use formal methods?

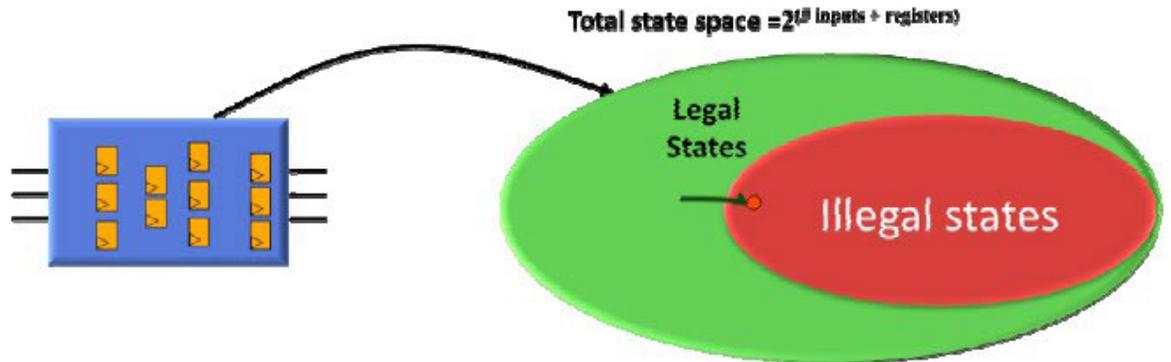
Many people are very intimidated by the thought of formal methods. They may have learned a little bit about it in their college days in a very academic sense only. At the same time, they've been using simulation for many years. How to run simulation is well understood.

However, if you stepped back and really examined how a simulator works alongside how a formal methods engine works, formal methods actually are simpler in concept.

However, formal methods often suffer from a legacy stigma as being a method only suitable for those who have a Ph.D., or at least a propensity for math. While this may have been true 20+ years ago, before commercial tools, RTL coding standards, and property specification languages, today it is simply an artifact of a time gone by. The creation of intuitive user apps leveraging sophisticated formal engines has drastically lowered the barrier of entry to use formal methods.

How formal methods find bugs

It's perhaps natural that some misconceptions about formal methods remain. After all, the very idea that a commercially available tool can readily take a RTL design and a simple-to-specify property and exhaustively verify its functional correctness sounds impossible. Simply put: It sounds too good to be true. As a result, many people are skeptical that it really does exist. With that in mind, let's try to explore how a formal tool can find bugs in a design.



First, think of a design as a collection of registers and input pins. For standard digital designs, when you change the input stimulus and apply a single clock, the state of the design will change. That is, the design will change its behavior and do something different. Change the inputs, give another clock, and the design state will change again. As long as the design keeps doing things that are expected and meeting its requirements, it's operating within its "legal state space."

On the other hand, if the design ever does something illegal that violates its requirements, we can say the design has moved into "illegal state space," and the design has a bug.

Simulation works fairly intuitively. It walks through the design's behavior changing input signals, giving a clock, changing input signals, giving a clock, etc. Repeat this process until the simulation test reaches its end, where some output value is typically compared against an expected value. If the output value matches its expected value, the test is said to "PASS." If not, then the test "FAILED." It makes perfect sense. One can even perform this task manually by tediously propagating values through the design to determine what the design will do next.

The key problem to this approach is obvious to anyone that has functionally verified a design of any complexity. If the collection of simulation tests fails to exercise some portion of the design, then a bug may exist that was previously unknown. In some cases, this could be an unexpected combination of conditions that is difficult to predict.

Formal verification does things a bit differently. Formal flips the entire problem on its head. By using a property to directly define legal vs. illegal state behavior, formal asks the question: "Is there any possible way to get from a legal state to an illegal state?"

To perform this analysis, formal starts with a single state, which is typically the "reset state" (the state reached after the reset signal is applied). Formal then thinks about all the possible behavior, all the combinations and permutations of 1s and 0s across all input signals. It calculates how the design will behave as a result of each and every one of these inputs and remembers the result. Then for each one of these results, formal again considers each and every possible input combination and permutation, and how the design will respond, again remembering all results.

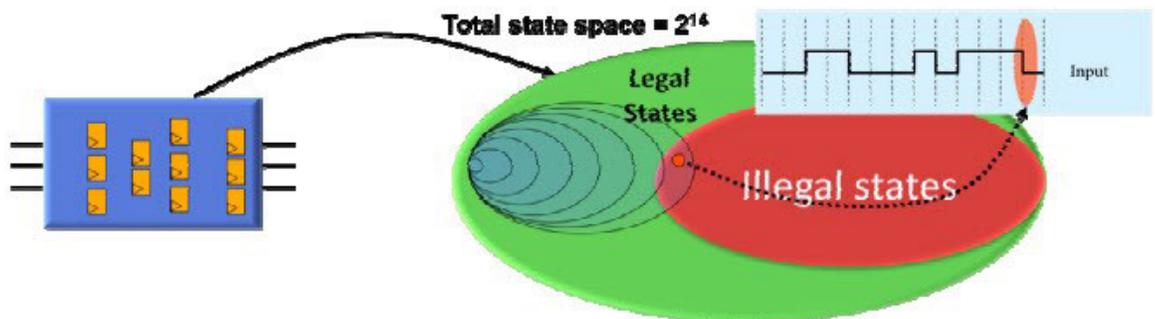
At each result, formal asks itself, “is this result illegal with respect to the specified property?” If so, then the tool has found a way that the design doesn’t meet its requirement, and it is reported to the user. If not, the procedure continues. Eventually, formal will realize that it has examined all possible results, indicating there is no illegal behavior possible, and a “proof” of correctness results.

Requirement	Description
Reverse_thrusters_001	Reverse thrusters shall never deploy in flight
<pre> property reverse_thrusters_001; @(posedgeclk) activate_rev_thrusters -> weight_on_wheels assert property reverse_thrusters_001; </pre>	

For the example requirement below, the property simply states that “if we currently see activate_rev_thrusters, then it implies that we must already have weight_on-wheels.” If not, then we’ve reached an “illegal state space.” This is using the IEEE industry standard SystemVerilog Assertion language.

As you can imagine, the number of results the tool needs to compute and remember grows exponentially. It’s only in the past 10 years that very clever formal algorithms, combined with very fast computers, have allowed formal methods to be applied in practical ways.

Hopefully this has somewhat de-mystified the formal methods process. With this basic understanding in mind, we can now move on to explore the DO-254 spec related to this topic.



DO-254 Appendix B 3.3.3 Formal methods explained

This section examines the actual text of Appendix B, 3.3.3, looking at exactly what is written, in the order it is written, and explaining it one small piece at a time. Information that is pulled directly from DO-254 is highlighted in blue text for clarity.

Formal methods definition

The text of DO-254 says:

3.3.3 Formal Methods

The term formal methods refers to the use of techniques from logic and discrete mathematics in the specification, design and construction of computer systems.

Note: The material in this section is derived from “Formal Methods Specification and Analysis Guidebook for the Verification of Software and Computer Systems, Volume II: A Practitioner’s Companion,” May 1997, NASA-GB- 001-97. A more detailed presentation of the application of formal methods, illustrated with a worked example, can be found there.

As previously mentioned, formal methods are mathematical methods. They use the proven principles of mathematics as the foundation of their analysis.

Also look at this note. This basically says that the information in this appendix is taken from a publication from 1997 that focuses on software and computer systems. Later in this paper we will talk about the changes that have occurred since the mid-90s and the status of usage today. Later in the paper, we will also clarify the differences between formal verification of software and hardware, because they can be significant in terms of practical application.

Two types of formal

Applications of formal methods fall into two broad categories, descriptive and deductive. Descriptive methods employ formal specification languages, which provide for clear, unambiguous descriptions of requirements and other design artifacts. Deductive methods rely on a discipline that requires the explicit enumeration of all assumptions and reasoning steps. In addition, each reasoning step must be an instance of a small number of allowed rules of inference. The most rigorous formal methods apply these techniques to substantiate the reasoning used to justify the requirements, or other aspects of the design or implementation of a complex or critical system.

Value of formal

The purpose of formal methods is to reduce reliance on human intuition and judgment in evaluating arguments. That is, deductive formal methods reduce the acceptability of an argument to a calculation that can, in principle, be checked by a tool, thereby replacing the inherent subjectivity of the review process with a repeatable exercise.

This text clarifies the value of formal, and why it is important. Formal methods provide a mechanism for automating analysis that is simply too difficult to do manually because it would depend too much on a person's intuition and judgment – which can certainly vary from person to person, yielding perhaps different and incomplete results. Formal is consistent, complete, and repeatable.

As an analogy, using formal to verify a hardware design is not much different than using a calculator to solve a math problem. Both utilize the principles of math, automate a difficult problem, and even if the underlying technology is not well understood by the masses, this doesn't stop the tool from providing significant value. Hence, you do not need to be a math expert to apply formal methods.

Formal approaches for design assurance

The next part of the Appendix B text begins to discuss how Formal plays a role in improving design assurance.

There are several areas where application of formal methods provides additional assurance in the design process. Although formal methods are applicable throughout the design process, increases in design assurance may be obtained by targeted application. The following list highlights some of the possibilities:

1. Early stages of design
2. Entire design, specific components, and other uses
3. All functions, important properties, unintended behavior

Early stages of design

Formal methods may be applied at different stages of the development life cycle. Generally, applications of formal methods are most effective at the early stages of the life cycle, specifically during requirements capture and high-level design.

This is referring to the use of formal at the earliest stages of design, such as requirements capture and conceptual design.

System architects often use formal methods as they are evaluating early system models and possible architectures. Since DO-254 is currently scoped (through AC20-152) to the component (PLD, FPGA, ASIC) level, this is an interesting fact, but not necessarily something you will see done at the conceptual design of the component—the system perhaps—but not the component.

On the requirements side however, formal can play a vital role, even if scoped to the component level. We will see in a moment how formal is linked tightly to requirements, and why this is such an important aspect of the value provided by formal. But for now, suffice it to say that in translating requirements to a formal language, this can lead to bugs or issues in the requirements being found very early in the design process – during requirements capture and validation-- where they pose minimal cost and schedule risk.

Entire design, specific components, and other uses

Formal methods may be applied to the entire design or they may be targeted to specific components. The FFPA is used to determine which FFPA to analyze with formal methods. Protocols dealing with complex concurrent communication and hardware implementing fault-tolerant functions may be effectively analyzed with formal methods.

Formal methods may be applied to the entire design or they may be targeted to specific components. The FFPA is used to determine which FFPs to analyze with formal methods. Protocols dealing with complex concurrent communication and hardware implementing fault-tolerant functions may be effectively analyzed with formal methods.

In theory, formal can be applied to the entire design. However, a reality of design complexity and tool capacity is that unless the design is fairly small, applying formal to the whole design is not generally practical. Today, it is far more common to see formal applied to specific components, or rather, blocks of the design. Here the problem space is much more conducive to an exhaustive verification approach.

Another interesting approach to using formal would be to provide added assurance (verification) to the safety-specific aspects of the design, such as the functional failure paths and safety-critical functions.

Another sweet spot for formal use today is in verifying very complex hardware, especially with concurrent functions. Likewise, formal could be used to validate the correct operation of fault-tolerant functions, ensuring it is indeed completely resistant to fault conditions.

All functions, important properties, unintended behavior

Formal methods may be applied to verify system functionality, or they may be used to establish specific properties. Although formal methods have traditionally been associated with “proof-of-correctness,” that is, ensuring that a component meets its functional specification, they can also be applied to only the most important properties. Often, it is more important to confirm that a design does not exhibit certain undesirable properties, rather than to prove that it has full functionality.

This indicates that formal can be used to verify all system functions or just some of them, perhaps only the most important. Again, this goes back to scoping how formal is being used. Will it be used for all properties, to exhaustively verify the entire design? This is possible, but as mentioned before, it’s generally not a practical approach. More likely, formal will be used to verify a select set of properties, usually those of most concern.

During the course of verifying properties, formal also provides a unique side benefit – it finds unintended behavior. This is something very difficult to achieve with a simulation-only approach. This is where “reliance on human intuition and judgment” is not good practice. Instead, using an exhaustive mathematical analysis can provide tremendous value in safety-critical designs. We will talk more about how this is done in future sections.

Formal tools and tool assessment

Practical application of formal methods typically requires tool support. Tools used should be assessed and, if necessary, qualified as described in Section 11.4.

This should come as no surprise to anyone. You need tools to run formal analysis. These tools should not be treated any differently than any other verification tools used in the design flow.

It is not uncommon to hear the objection “How can we trust the results, if we don’t understand how the tool works?” But think about it. How many people really understand how simulator algorithms work, or the circuitry within a calculator for that matter? Very intelligent people, who do understand how these things work, have engineered these products for the benefit of the masses.

Now, this does not mean they should simply be trusted. There should be no “trust” in a DO-254 program. No two tools, just like no two people, are alike. That is why all work must be reviewed, double-checked, or proven worthy of the task.

Two main approaches can be used for assessing formal tools.

1) Independent output assessment

As we will see in a bit, simulation and formal methods are complimentary. They are generally used together in a flow. In many ways, they approach the verification problem very differently and, in this regard, provide different ways of looking at the verification problem. Verification flows that use both typically have some amount of overlap and double-checking. This double-checking can also be explicitly done if there are concerns about the tool outputs.

In addition, throughout a DO-254, each stage of design requires additional verification. Formal methods are usually done early in the design process. Numerous other verification methods and techniques will also be run later in the process, on models of lower abstraction levels, on the HW item itself, and with the HW item in the target system. Each of these additional verification methods and processes should be verifying previous verification work. A good DO-254 flow will automatically have these checks and balances (that support independent output assessment) built in. This is the best approach.

2) Qualification kits

It would also be possible to provide a set of test cases that could ship with the tool. These test cases could run in both simulation and formal to explicitly force both types of tools to verify the cases. The results of both should match.

While this is certainly just a tiny fraction of the sort of testing that is done on these tools by their developers, and therefore the value of this sort of process is highly questionable, if certification authorities required it, it could be done. Tool vendors or the hardware applicant could come up with such a test suite.

Requirements, properties, and assertions

3.3.3.1 The Methodology of Formal Methods

The application of formal methods begins by expressing the requirements using a formal language. The requirement specification serves an important descriptive function. It provides a basis for documenting, communicating, and prototyping the behavior and properties of a system using an unambiguous notation.

Finally, we are able to tie formal methods to a requirements-based design process. We start by defining some terms so we can see how formal methods works and how it can truly be a requirements-based verification approach.

A requirement is a description of design intent/behavior. The customer, architect, or designer (all the people who may have a hand in writing requirements) usually writes requirements in their native language (such as English). The problem with this is that native languages like English are very ambiguous, and prone to various interpretations. Even though requirements are reviewed and validated, oftentimes, bugs later in the process tie back to misinterpretation or misunderstandings of the actual intent of a requirement.

With formal methods, an engineer must translate the native language requirement into a formal language description of this requirement. The formal description of a requirement is called a property. A property specifies a requirement unambiguously in a formal language that enables tool use. Because the formal language is unambiguous, the tool can interpret the property only one way.

One of the major barriers to adoption of formal methods prior to the year 2000, was the lack of standardization of these formal languages. Today, the industry has adopted two languages for the specification of properties: PSL (Property Specification Language, IEEE 1850) and SVA (SystemVerilog Assertions, IEEE 1800). As IEEE standards, this ensures that a whole industry

infrastructure exists for their support (documentation, libraries, tools, training, etc.).

The property is merely a mechanism to formally capture design intent. In order to tell a tool that you want to do something with a property, such as monitor it during simulation, and check it with formal verification, you must assert it. Thus, an assertion is a tool directive to “turn on” a property for verification.

An example can make this more concrete. Suppose you have the following design requirement from our earlier example.

An example can make this more concrete. Suppose you have the following design requirement from our earlier example.

“The reverse thrusters shall never deploy in flight.”

This can be formally described as a property (in this case, using SVA) as follows:

```
property REVERSE_THRUSTERS_001;  
@(posedge clk)  
  
activate_rev_thrusters |->  
weight_on_wheels_notification;  
  
endproperty
```

This description will passively sit in the code (i.e., the design code or a separate verification file) doing nothing until you decide to use it in verification. You do this through an assertion as follows:

```
property REVERSE_THRUSTERS_001;  
@(posedge clk)  
  
activate_rev_thrusters |->  
weight_on_wheels_notification;  
  
endproperty  
  
assert property REVERSE_THRUSTERS_001;
```

The “assert” keyword triggers the simulator to monitor the property during simulation. Likewise, all asserted properties are checked when formal runs.

Formal model and analysis

In addition, the requirements specification serves as a basis for calculating or formally predicting system behavior. A formal model of the component to be analyzed is constructed using a formal language. The model is analyzed with respect to the formal statement of requirements using the rules of the selected formal logic. The characteristics of the model are determined by the style of formal analysis to be performed.

As we have just demonstrated, requirements become a key aspect of formal analysis when they are written as properties and asserted. Next you need a formal model.

This is another key area of misunderstanding with regards to formal use in hardware. You do not need a separate model to be used for formal analysis. The formal model is simply the RTL model, which in the military/aerospace industry is typically VHDL code (or Verilog, SystemVerilog, mixed languages).

How or why can the RTL be used as the formal model? Consider this. To simulate the model, you have to compile the VHDL code into a set of primitives or C code that is executed by the simulator. This is the same with synthesis – the RTL model is compiled into a gate-level model. Similarly, with Formal, the RTL model is compiled into a mathematical model. They all start from the same RTL model and translate it to the internal model appropriate to fulfill their task.

The formal analysis process compares the model (e.g., the VHDL) to the requirement (via the assertion), calculating whether the requirement is true within the model.

The level of detail in the component model is determined by the goal of the chosen formal analysis technique. Some approaches are tailored to finding design errors that may have eluded testing, while other approaches seek to guarantee the absence of certain classes of design errors.

For use in DO-254 projects, the formal model is the RTL model (e.g., the VHDL code). A number of formal techniques can be used on this model, including searching for bugs (i.e., bug hunting) versus trying to exhaustively prove no bugs exist (i.e., assurance). Both find bugs, but the goals are different. The first approach attempts to quickly identify bugs in a non-systematic fashion using formal techniques. The second approach is a comprehensive and systematic methodology to achieving assurance, at a potential cost of more effort and time.

(Formal) model checking

1. **Error-Detection.** The most common formal technique for error detection is called model checking. Here the requirements are expressed as formula in a decidable temporal logic. The model of the component is an abstract state machine designed so that the property to be tested is preserved. The proof procedure is automatic. A failed proof attempt indicates a design error in the modeled component. The result of failed proof is a sequence of input stimuli that demonstrate specifically how the component does not satisfy the stated requirement.

Formal model checking, or simply model checking, is the formal analysis process we just introduced. In this common use of formal methods, a formal analysis tool checks a design model against its requirements. The output of model checking includes proofs or failed proofs. We will talk about this more in section “Outcomes of Formal Model Checking.”

Model checking compliments simulation

Something that is important to understand about model checking is that it should generally not take the place of simulation, but rather be used alongside of it.

In the early days of commercial formal tools, companies that sold these tools believed so strongly in their verification abilities that they often promoted these solutions as the replacement for simulation. However, as the use of formal has become more common place, it has also become more and more apparent that both simulation and formal analysis are necessary to ensure a design is thoroughly verified. Thus, the vast majority of companies who use formal today do so in a manner that is complementary with simulation. This is because both simulation and formal analysis have their sweet spots, and pitfalls.

Simulation allows you to create and verify just about any type of circuitry or situation that you are creative enough to think of. It operates with a model of the design environment (called the test-bench) sending stimulus (or test cases) to the model of the design (called the device under test, or DUT), and checking the model’s response. The simulation test environment is typically developed by one or more verification specialists. Simulation is very flexible, but the tests are only as good as the skill of the verification team creating them.

Simulation is rarely, if ever, exhaustive (except for the most simplistic of circuitry). For today’s large designs, simulation might demonstrate the presence of a bug, but unlike formal, it can never prove the absence of a bug.

Formal model checking does not require a testbench or any input stimulus. The test cases are simply the assertions that are written from the requirements. This enables testing to start much earlier in the process because far less infrastructure is needed. Often (but not always) this early testing is done by the designer himself. In this regard, the designer is checking his code (part of the model) a bit at a time, against the pertinent requirements. The assertions can be reused for official verification work done independently by verification team. These assertions can also be used during the simulation activities that are done by this team (note that this is a very common practice, but somewhat beyond the scope of this specific paper). The drawback with formal is that it is a highly intensive computational process that consumes huge amount of memory and computing power. For this reason, it is best used at the block level of design, is best suited for certain types of circuitry (this is elaborated in “Where to Use and Not Use Formal”) and may benefit from requirements being broken down into multiple, smaller assertions. If scoped and used appropriately, formal provides exhaustive analysis. Formal also runs much more quickly than simulation.

The following table summarizes the use of simulation and formal methods (including how they are different, and how they complement each other) for verification:

Issue	Simulation	Formal
Model (DUT)	RTL (e.g., VHDL)	RTL (e.g., VHDL)
Testbench	Required	None
Test cases	Usually hand created	Automatic (via assertions)
Types of Circuitry Supported	Just about all	Some better than others
Design Level	Block or Top Level	Block Better
Exhaustive	No	Yes
Linked to Requirements	Depends on testcases	Yes, requirements-based assertions
Support Assertions	Yes	Yes, required
Used for Early Verification	Prohibitive (infrastructure needed)	Well suited

Theorem proving

2. Error Preclusion. Formal methods targeted to prevention of errors are generally based upon an expressive specification language with a supporting proof theory. With the increased expressiveness, more complicated requirements may be stated, and more detailed models of the component may be constructed. However, the proof procedure may only be partially automated. An appropriate level of detail for the component model may be a synthesizable HDL description. In some cases, the same model may be used both for simulation and formal analysis. A completed proof is evidence that the component is logically correct with respect to the stated requirements for the analyzed input space.

This section of DO-254 is admittedly quite confusing. It is talking about a formal methods technique called Theorem Proving. While theorem proving is not uncommon for academics and Ph.D. types who focus on systems analysis and architectures (in fact “error preclusion” means trying to find bugs in the architecture upfront, prior to RTL development), it is unlikely to be used today on component level development in DO-254 compliant programs. Therefore, at this time, for the current scope of DO-254, this text is something that is not relevant.

Outcomes of formal model checking

3.3.3.2 Formal Methods Resolution

There are three possible outcomes of a deductive formal analysis:

1. If the proof attempt is successful, the verification activity is complete. The level of design assurance depends upon the fidelity of the models employed. For example, if the model of the hardware item corresponds to a detailed design, the proof provides assurance of functional correctness equivalent to that of exhaustive testing.
2. In some cases, a failed proof results in an explicit counter-example; that is, it identifies a test scenario to illustrate specifically how the design does not meet the stated requirements. This may indicate either a deficiency in the design or a deficiency in the requirements. Such deficiencies may be resolved by correcting the design, revising the requirements, shown to not be a physically realizable condition or using another method. All counter-examples should be identified so that they can be resolved. Changes to the design or requirements need to be reflected back to the appropriate process.
 - a. After a design or requirement has been modified to address a deficiency identified by a failed proof attempt, the proof should be attempted again to confirm that the modification has successfully addressed the identified problems. This cycle is repeated until a successful proof is achieved.
 - b. In cases where a counter-example is considered resolved without requirement or design changes but the tool identifies only one counter-example, that is, the resolved counter-example, the process should be modified so that it can identify all other counter-examples.
3. The most difficult case to resolve is when a proof cannot be produced and a counterexample cannot be identified. One possible option is to revise the

design in order to simplify the verification effort. Alternatively, the verification activity may be decomposed with a clear delineation between the cases addressed by proof and those cases where the requirement needs to be addressed by some other means. Changes to the design and derived requirements should be reflected back to the FFPA.

This is a lot of text to say something rather simple. Basically, model checking produces one of three outputs as follows:

- Proof
A proof provides evidence that exhaustive analysis reveals that a model will always operate according to the requirement (no exceptions).
- Counter-example
An exception is found. Each counter-example provides a waveform (that can be used in simulation) that demonstrates a condition where a model violates a property. Usually a counter-example indicates unintended behavior of the design.
- Inconclusive
This situation indicates that given the current conditions, a tool is unable to come up with one of the previous options. Thus, more verification work must be done. This typically involves breaking down the problem to something simpler, either by scoping the amount of circuitry being analyzed or breaking the requirement down into multiple smaller requirements.

If you would like a better understanding of how model checking works, and the algorithms employed to come up these results, numerous papers and publications are available that describe this. For example, Siemens EDA has lots of content and webinars related to formal verification at: <https://eda.sw.siemens.com/en-US/ic/questa/formal-verification/> .

Formal methods data

3.3.3.3 Formal Methods Data The data developed during the application of formal methods includes:

1. Description of the specific formal methods approach to be used and the components or FFPs to which formal methods will be applied.
2. Formal statement of requirements.
3. Formal models of the component.
4. Proof, or sufficiently detailed script to generate proof, relating the models of the component to the formal statement of requirements and including correlation in the traceability data.
5. Identification of tools employed and tool assessment results.
6. Identification of the verification test cases and requirements added or modified as a result of the analysis.
7. Statement of the level of the verification completeness achieved for the FFPs addressed by analysis. Include a list of the analysis discrepancies not resolved by modification to verification test cases or requirements and their rationale for acceptability of the discrepancies.

This text tries to clarify the types of data that must be created and reviewed if formal methods are to be used in a DO-254 project.

Formal Data Checklist

The following list explains this in more detail. You can use this list a checklist for the data that should be used and review when formal methods are used on a DO-254 program.

1. Description of the formal methods approach
The section entitled “Formal Use Models” describes some of the ways that people are using formal methods today. In terms of the DO-254 project, the Verification and Validation Plan document should capture a description of how specifically formal is being used on the project. It should

cover who is using formal methods, at what stage of design, on which blocks/circuitry/properties and for what purpose.

2. Formal statement of requirements (i.e., properties)
The formal descriptions of requirements are the design properties, written in an industry standard property language, such as the IEEE-1850 PSL or the IEEE-1800 SVA. The property should be thoroughly reviewed (alongside the requirement), documented and linked to its corresponding requirement. Note that in some cases, a requirement may have more than one corresponding property.
3. Formal model
The formal model is just the VHDL (or Verilog, or SystemVerilog) design code. No modifications are necessary. This model is already part of the design flow and should not be treated any differently as it would be for simulation or other verification activities.
4. Proofs, results, traceability
Proofs, along with the repeatable scripts/methods that generate the proofs, should be captured in documentation, reviewed, and perhaps even demonstrated during reviews or audits. The proofs are considered the verification results and thus complete the traceability loop from requirement to property to process (script) to results (proof).
5. Tools and assessment
Just as any other design or verification process, the tools and assessment methods must be documented in the PHAC or V&V Plan. Since formal methods will typically be used alongside simulation, and in fact the formal methods tool produces test cases (in the form of counter-examples for simulation) for simulation, a typical approach may be independent output assessment via simulation.

6. Counter-examples, new tests, new properties
 Achieving a full proof may not occur on the first try. For example, when the formal tool discovers design behavior that violates a property, the tool produces a counter-example (i.e., a waveform) that demonstrates the unintended behavior. This counter-example can and should be run in simulation, and in fact can be added to the simulation test suite as a new test for regressions. These sorts of new tests should be documented and treated the same as other simulation tests (i.e., reviewed, traced, etc.). At other times, a property may be too difficult to verify as it stands (e.g., the tool may run out of memory trying). In these situations, the property may need to be broken down into multiple properties, or similarly, a property may need to be run first within smaller portions of the design. When these situations occur, they should be documented and reviewed.

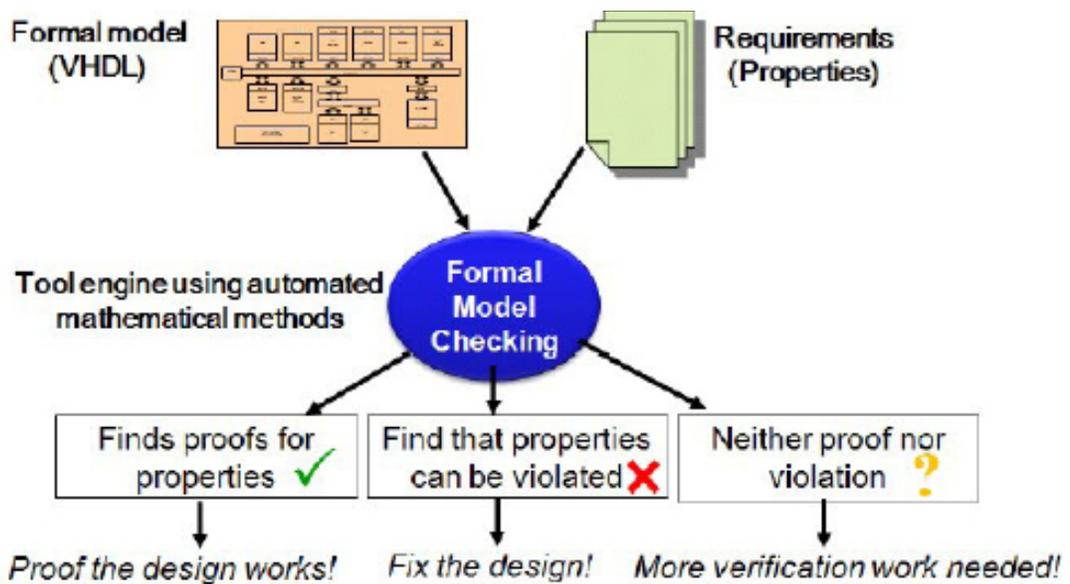
7. Formal methods results
 The V&V Plan stated the intent of formal methods, including the use model and goals. Perhaps the intent was to exhaustively verify a handful of safety-critical properties. When formal methods

analysis is complete, the results (in this case, formal proofs) should be reviewed against the goal to ensure the goals were met. In this example, if a proof was achieved for each safety-critical property, then the goal was met. If not, most likely steps were taken as described in step 6, which should all be documented. If a targeted property (or block or structure) has not been thoroughly verified via formal methods as per the plan, justification should be made as to why it is not necessary, or which alternative verification methods will be employed to ensure an appropriate level of testing.

**Summary of Appendix B,
 3.3.3 Formal Methods**

Formal methods is a mathematical analysis approach. Model checking (a common type of deductive formal analysis) automatically verifies a design model against requirements. Model checking can improve design assurance by exhaustively verifying circuitry and finding unintentional behavior. Note that model checking is complementary to simulation.

The following figure provides a visual summary of the model checking process:



I Today's use of formal

This section examines the state of the industry today, including the evolution of formal methods for hardware over the last 20+ years, who is using it today, how are they using it, and why.

A bit of tool history

The development of commercial formal methods tools for hardware began in the late 1990's. Prior to this, the only tools available for formal model checking were developed in academia and never commercialized due to numerous impracticalities and inadequacies (such as user interfaces, integration with existing flows, standards, use models, marketing and support).

One of the first companies to focus on developing commercial formal model checking tools was 0-In (acquired by Mentor Graphics and now part of Siemens EDA). By early 2000, 0-In had launched several commercial model checking products, and since that time numerous products and apps have been produced along with quantum leaps in solver technology capabilities. Around this same time, several other companies (Cadence, Synopsys, Averant, Real Intent, OneSpin) followed suit. Since then, the market has grown from virtually nothing to around \$300M.

Industry data

The Wilson Group Survey is done every two years and reveals significant growth in formal. The 2020 analysis of the ASIC and FPGA markets reported significant growth for both property checking and formal apps. For the ASIC markets, property checking has a four year CAGR of over 8%, and the formal apps over this same period has a 19% CAGR. The FPGA market for property checking has a four year CAGR of 5% for property checking and a four year CAGR of 12% for the formal apps. This indicates that people are using formal methods today, often as plan of record, and usage is on the rise.

As a commercial vendor of formal analysis tools, Siemens EDA has witnessed these same trends. Today we have a large number of formal model checking tool customers, many of whom are currently using these tools on DO-254 programs.

Why people are using formal

Regardless of the particular use model or methodology, by far the number one reason people use formal is for improved quality. Improved quality means more assurance that the design operates as it should. Thus, formal is primarily used today to improve design assurance, which is the driving force behind DO-254 compliance.

Another benefit of formal is that it's much easier to tie formal verification activities to design requirements – after all, that is what model checking does. It checks a model against requirements for that model. With simulation this is harder. You can certainly write tests that map to requirements, but it's much more difficult to ensure you have thoroughly tested a requirement with simulation. With formal, you exhaustively test a requirement, or you find situations where the requirement is violated. These examples of violations demonstrate unintended behaviors of the design, which is again difficult to find with simulation. Certainly, you might get lucky and find these things with simulation, but formal provides conclusive, exhaustive evidence of these behaviors (and waveforms demonstrating the behavior that you can double-check in simulation).

People are using formal more and more these days because the majority of barriers have been broken down. Previously, no standard assertion languages existed. Today we have IEEE-1850 (PSL) standard and the IEEE-1800 (SVA) standard. A whole industry infrastructure now supports these standards,

including tools, support, consulting, documented use models, etc. There are even standard libraries of pre-written and verified assertions that use these languages, so even the learning curve has been tremendously minimized.

Best of all, people are using formal methods today because finally, it does not take someone with a Ph.D. in mathematics who understands the underlying algorithms of the tools to reap the benefits of these tools!

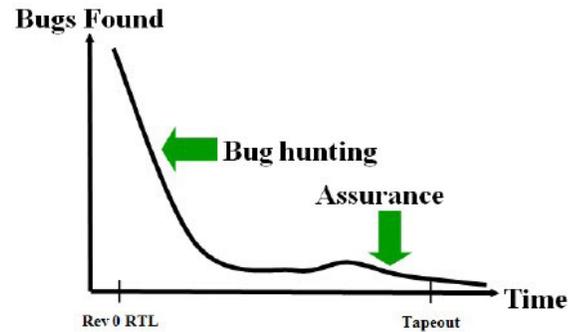
Formal use models

Through working with many customers over the years at Siemens EDA, we've seen over 17 use cases of formal! This demonstrates that companies have found a lot of interesting ways that formal model checking can add value to their verification methodologies. However, 17 is a lot to digest. In this paper, we will consider two main categories of formal model checking usage, and then list six main use models, describing what they are and identifying some of the companies that use formal in these ways.

Bug hunting and assurance

Formal model checking can be broken down into two main categories: bug hunting, and exhaustive proof for design assurance (referred to from this point on as simply assurance). These categories were briefly introduced in the section entitled "Formal Model and Analysis." Here we will describe them in a bit more detail.

The following picture visually conveys various facets of these two approaches.



The X-axis depicts time, or more precisely, the design schedule, with earlier design activities happening on the left and later activities on the right. The Y-axis represents the bug rate on a project.

For example, bug hunting is an approach that can occur from the early stages of RTL development. Designers can use assertions to test their code (usually at the block or sub-block level) very early on in the process. This will be an early and highly iterative process to ensure high quality code is developed from the start. Many (typically low level) assertions will be used and will find many bugs. The focus of this approach is on productivity; that is, finding as many bugs as possible as quickly as possible.

On the other hand, as the code firms up and the design comes together, the verification team may want to verify the design's behavior by exhaustively checking important properties (usually at the design level). This method will require more focused attention, and catch fewer bugs, but these sorts of bugs can be very serious in nature. The focus of this approach is on assuring that the design meets the specification and is thus, of high quality.

Most of the formal use models lean more towards one of these approaches than the other.

Six primary use models

The following list describes today's six most common formal use models:

- Architectural verification
As previously mentioned, this is usually done by a formal verification expert, very early on in the design's conceptual development (usually at the system level model), and generally uses theorem proving techniques. Thus, this use model is not commonly found (or at least, not commonly visible) in DO-254 programs.
- White-box sanity checking
White-box test refers to the idea that you can see inside the design code as you're testing it. Thus, it is usually the designer himself that uses formal in this way as a method to do early analysis of the RTL code. The designer would create a number of assertions (or use assertion libraries) that test his code (and the complex structures within it) and ensure it operates as he thinks they should.

This usage model is similar to early sandbox testing with simulation. As such, this method would likely be considered as per Note 2 in DO-254 6.2:

"Informal testing outside the documented verification process is recommended. The procedures and results, however, are not necessarily maintained under configuration management control but are highly effective in the detection and elimination of design errors early in the design process. Verification credit can be taken for this testing only if it is formalized."

So while generally not part of the official DO-254 verification activities, this use model can be an essential part of ensuring that the early code is verified as it is developed and thus comes together clean and bug-free at integration. Companies such as Siemens, Sun (formerly), Qualcomm, Dice, SLE, and Alcatel-Lucent are known to use formal methods in this way.

- Implementation Protocol Verification
Today's designs often contain components that utilize and support complex protocols, such as PCI express, USB, AMBA, SATA, DDR, and so on. Because these are commonly used, companies (such as Siemens EDA, and other suppliers of verification tools or services) have created pre-designed and verified packages of assertions that can be used directly to verify these complex protocols. (This model is similar to design intellectual property, but these pre-packaged assertions are called verification intellectual property, or VIP)

This use of formal can be done by either the designer or the verification engineer. In either case, it requires little to no knowledge of assertions, languages, or formal methods. It is all very automated. It also has elements of both assurance and bug hunting, depending on who is running the testing and at what stage of design. A large number of companies use formal in this way, including Infineon, Saab, National Semiconductor, MediaTek, Brocade, Evatronics and ARM. This use of formal would be visible as part of the verification process (most likely, for credit) in a DO-254 project.

- Black-box (or Grey-box) Testing
This method is predominantly an assurance approach, where there is a formal test plan that identifies the properties that will be verified, and the goal is exhaustive proof attainment. A verification engineer (and typically one that is experienced in formal methods) will be the main person running formal model checking in this way.

Companies known to use this approach include DE Shaw, SLE, nVidia, AMD, IBM, ST and Infineon. This use of formal would be visible as part of the verification process (definitely for credit) in a DO-254 project.

- Coverage Analysis

In some cases, it can be very difficult to set up all the conditions to stimulate a design and examine the response – especially in test complex circuitry. When these situations are known, then formal is a good alternative to simulation to verify these parts of the design. Typically, it is the verification team who understands this and opts for this use model of formal to augment and assist in closing the coverage holes of simulation. Formal can generate simulation scenarios that can be captured and used as tests in the simulation test suite. Companies that use formal in this way include Sun (formerly), Tensilica, Alcatel-Lucent, Azul, MetaRam, AMD and Hewlett-Packard. This use of formal would be visible as part of the verification process (most likely, for credit) in a DO-254 project.

- Post-silicon debug

Formal can also be used late in the process to assist in silicon debug. When bugs are found in the lab, they can be extremely difficult and time-consuming to debug. However, it can sometimes be fairly easy to write an assertion to mimic the behavior seen in the lab and then run formal verification to flag what is causing it. Either the designer or verification engineer may become involved to write the assertion and debug the RTL design. At Siemens EDA, we know that a number of companies use formal in this way, but most do not want to publicly acknowledge it (since having bugs escape verification and not be caught until silicon is not the ideal situation). This use of formal would likely not be visible and not used for verification credit in a DO-254 project.

Where to use and not use formal

It was once thought that formal would replace simulation. After years of pushing this message and learning where formal was strong and where it was weak, the industry (and most commercial tool vendors) now concede that formal methods have strengths and weaknesses in terms of where they should be used.

A key paper that identified these suggested areas in which to use or not use formal methods was “Guidelines for creating a formal verification test-plan,” by Harry Foster, Lawrence Loh, Bahman Rabii, and Vigyan Singhal at DVCon 2006.

What follows is a summary of the ideas presented in this paper.

When and where to use formal methods:

Control or datapath circuitry with high concurrency (and no data transformations)

- Arbiters
- On-chip bus bridges
- Power management units
- DMA, interrupt, memory controllers
- Bus interfaces
- Schedulers
- Standard interfaces

When and where to avoid formal methods:

Datapaths with data transformations

- Floating point units
- MPEG decoder
- Convolution unit in DSP
- Graphics shading unit

In general, formal model checking works best on control circuitry, datapath circuitry (unless it involves data transformations), and circuitry with complexity due to concurrency. These are areas that are particularly difficult to write tests for simulation.

These types of circuits also tend to harbor complex, corner-case behaviors. Formal is especially useful in these situations.

On the other hand, formal is not good in dealing with circuitry that is “often sequential in nature” or “potentially involves some type of data transformation” such as floating point units and MPEG decoders.

Formal in software vs. hardware

Many people confuse the formal methods for hardware with formal methods for software. This is understandable. The principles are identical. What differs is in the practical application.

Using formal methods in software is more challenging and less practical than in hardware for several reasons.

First, the software side offers no “formal friendly” coding standards. On the contrary, in hardware the industry has been forced to come out with standard ways of writing VHDL (Verilog and SystemVerilog) code that must be followed for synthesis. This same subset of these languages (referred to as RTL coding) is not only formal friendly, but it is the way that people have to design to use other tools in the flow. Thus, the same design model developed in “Detailed Design” and simulated can be used for formal. In the software domain, typically a whole new model is created and then this model has to be verified against the “real” model, just adding woe to the design process.

Second, in hardware we are dealing with simpler static models (finite state machines) while software must deal with dynamic structures and more complex infinite state models.

Software can expand and contract on-the-fly, creating new structures that require verification within the scope of their parent process. Hardware, by its very nature, is a fixed number of transistors connected in a fixed manner. As a result, the hardware being verified is fixed and static, and the application of formal verification is greatly simplified.

Finally, formal methods have been used to some extent on hardware for 30+ years. The algorithms to do the mathematical analysis of the hardware models are well understood, and today’s tools contain many self-checks within them.

Thankfully, formal methods in hardware is an easier problem to solve and a much more practical methodology to employ than in the software domain.

Still, despite these challenges on the software side, the value of formal methods is understood well enough that some government programs are now requiring secure software applications to be formally verified. Similarly, Microsoft formally verifies all its device drivers³. Also, some of the higher-level systems design analysis tools (such as Mathworks⁴) commonly use formal analysis in the verification of their models. This is common practice and in fact many DO-254 projects use Mathworks as the front-end of their design flows, so knowingly or not, they are likely using formal methods.

Misconceptions and objections

This paper should have cleared up the vast majority of these misconceptions. However, to summarize, here are a number of the common misconceptions and objections to the use of formal methods for DO-254 programs.

- Formal replaces simulation (a proven method)
On the contrary, in nearly all applicants, formal compliments simulation. Only in very rare circumstances would it replace simulation entirely.
- You have to use formal on all properties
You can use formal on any properties you want, some or all. We recommend that formal be used on the most critical properties and/or those that are difficult to fully verify using simulation.
- Formal algorithms are not well understood and can't be trusted
Most people don't understand simulator algorithms either, and yet, simulation is widely used and accepted.
- Since they can't be understood, Formal tools must be qualified
Formal tools could be qualified if that's what the applicant chooses. However, the usage model is generally such that other verification at other stages of design will certainly catch any issues possibly missed by formal. Also, it is possible to have a flow where formal and simulation directly double-check each other.
- If designers create assertions, this violates independence
Assertions state what needs to be verified, not who or how it is to be verified. Independence can be achieved via review or by someone else actually running and reviewing the results of verification. Assertions that map to functional requirements should be reviewed alongside these requirements by the team validating the requirements. If a designer creates additional structural assertions that are reused in verification, someone else runs this verification and checks the results.

- With formal, you have to create a whole new model and that model must be verified This is not true. The formal model IS the VHDL (or Verilog or SV) design with no modification. This is the same as simulation.

Recommendations

- ALLOW applicants to use "Formal Methods" for DO-254 projects
Hopefully it is now obvious that "Formal Methods" definitely has a place verifying DO-254 Level A/B designs.
- Avoid tools that encourage a user to guide the tool toward a proof
This is mainly intended to ensure caution when applicants select a commercial tool. Some tools encourage an extreme amount of user intervention. This will make repeatable results more difficult to achieve and increase the possibility of user error.
- Before running model checking (for credit)
 - Decide up-front where formal will be used, and why
 - Requirements & associated properties should be reviewed (this includes properties used as constraints)
 - "sanity check" properties in functional simulation, paying special attention to constraints
- During model checking tool usage
 - Re-run formal after design or property changes
 - Be mindful of the "starting state" (typically reset)
 - Use as few constraints as possible
 - Note: The best proofs are obtained without constraints, but this may be unrealistic
- During certification, use the Formal Verification Checklist presented earlier in this paper

I Conclusion

Formal methods offer a very powerful verification technique that can go a long way towards improving design assurance. Unfortunately, the description of formal methods included in the DO-254 document serves to confuse rather than clarify how and when formal methods should be used in the context of a DO-254 project. This has not served the DO-254 community well as it has both discouraged applicants from its use for fear of the certification process and confused certification authorities who do not understand how or why it can be used and therefore are likely to discourage its use.

This paper clarified the content of DO-254 Appendix B, providing both applicants and certification authorities with understandable information regarding formal methods operation, usage, and usefulness. It described the value of formal and its support of design assurance. It discussed industry use of formal, citing recent industry studies and articles, and elaborated on some of today's usage models for formal model checking. And finally, this paper offered encouragement about the promise of using formal methods to improve the quality of DO-254 compliant designs.

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